## Self-diffusion of spherocylindrical particles flowing under non-uniform shear rate

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This work numerically studies the self-diffusion of spherocylindrical particles when flowing down an inclined plane. This system is challenging due to particles being nonspherical and because they are subjected to a non-uniform shear rate. We perform simulations for several aspect ratios and inclination angles, tracking the particle trajectories. Using the simulation data, we compute the diffusion coefficients D, and a coarse-graining methodology allowed accessing the shear rate spatial profiles  $\dot{\gamma}(z)$ . It enables us identifying the spatial regions where the diffusivity fully correlates with the local shear rate  $\dot{\gamma}(z)$ . Introducing an effective particle size  $d_{\perp}$ , we propose a well-reasoned scaling law between D and  $\dot{\gamma}$ . Our analysis also identifies specific locations where the diffusivity does not correlate with the shear rate. This observation corresponds to zones where  $\dot{\gamma}(z)$  has non-linear spatial variation, and the velocity probability density distributions exhibit asymmetric shape. Moreover, examining the velocity correlations, we obtain that the correlation length  $l_{\xi}$  is not constant, resulting shorter  $l_{\xi}$  values close to the bottom plane and higher  $l_{\xi}$  close to the free surface. Although our scaling analysis does not involve the particle correlation length  $l_{\xi}$ , our finding suggests that collective movement might play a crucial role in the self-diffusive dynamics.



Fig. 1. a) Trajectories of twenty randomly chosen particles after reaching the steady regime. b) Snapshot of the numerical setup; the red curve indicates the mean value of the *x*-component of the velocity profile along the *z*-direction,  $\bar{v}_x(z)$ . The figures correspond to the case  $\xi = 2.5$  and  $\alpha = 31.0$  degrees. The color of the particle quantifies the magnitude of its  $v_x$ . Note that gravity has an angle  $\alpha$  to the vertical direction, representing a slope with an angle of elevation of  $\alpha$  degrees.



Fig. 2. Ratio of diffusion coefficient and shear rate,  $D/\dot{\gamma}$ , plotted against the square of the characteristic particle length  $d_{\perp}^2$  for all inclinations  $\alpha$  and elongations  $\xi$ . The red points are the mean values of all  $D/\dot{\gamma}$  for each  $\xi$ , and the error bars indicate the standard deviation thereof. The black line represents the resultant linear fit. For all  $\xi$  values, a representation of the particle is illustrated.

- R. C. Hidalgo, B. Szabó, K. Gillemot, T. Börzsönyi, and T. Weinhart, "Rheological response of nonspherical granular flows down an incline" *Phys. Rev. Fluid.* 3, 074301 (2018)
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